

# Due date optimization in multi-objective scheduling of flexible job shop production

Ojstersek, R.<sup>a,\*</sup>, Tang, M.<sup>b</sup>, Buchmeister, B.<sup>a</sup>

<sup>a</sup>University of Maribor, Faculty of Mechanical Engineering, Maribor, Slovenia

<sup>b</sup>Beijing Jiaotong University, International Center for Informatics Research, Beijing, P.R. China

## ABSTRACT

The manuscript presents the importance of integrating mathematical methods for the determination of due date optimization parameter for maturity optimization in evolutionary computation (EC) methods in multi-objective flexible job shop scheduling problem (FJSSP). The use of mathematical modeling methods of due date optimization with slack (SLK) for low and total work content (TWK) for medium and high dimensional problems was presented with the integration into the multi-objective heuristic Kalman algorithm (MOHKA). The multi-objective optimization results of makespan, machine utilization and due date scheduling with the MOHKA algorithm were compared with two comparative multi-objective algorithms. The high capability and dominance of the EC method results in scheduling jobs for FJSSP production was demonstrated by comparing the optimization results with the results of scheduling according to conventional priority rules. The obtained results of randomly generated datasets proved the high level of job scheduling importance with respect to the interdependence of the optimization parameters. The ability to apply the presented method to the real-world environment was demonstrated by using a real-world manufacturing system dataset applied in Simio simulation and scheduling software. The optimization results prove the importance of the due date optimization parameter in highly dynamic FJSSP when it comes to achieving low numbers of tardy jobs, short job tardiness and potentially lower tardy jobs costs in relation to short makespan of orders with highly utilized production capacities. The main findings prove that multi-objective optimization of FJSSP planning and scheduling, taking into account the optimization parameter due date, is the key to achieving a financially and timely sustainable production system that is competitive in the global market.

© 2020 CPE, University of Maribor. All rights reserved.

## ARTICLE INFO

### Keywords:

Flexible job shop scheduling problem (FJSSP);  
Due date;  
Makespan;  
Capacities utilization;  
Multi-objective optimization;  
Evolutionary computation;  
Multi-objective heuristic Kalman algorithm;  
Simio simulation and scheduling software

\*Corresponding author:  
[robert.ojstersek@um.si](mailto:robert.ojstersek@um.si)  
(Ojstersek, R.)

### Article history:

Received 15 May 2020  
Revised 23 October 2020  
Accepted 25 November 2020

## References

- [1] Prester, J., Buchmeister, B., Palčič, I. (2018). Effects of advanced manufacturing technologies on manufacturing company performance, *Strojniški Vestnik – Journal of Mechanical Engineering*, Vol. 64, No. 12, 763-771, [doi: 10.5545/sv-jme.2018.5476](https://doi.org/10.5545/sv-jme.2018.5476).
- [2] Baker, K.R. (1984). Sequencing rules and due-date assignments in a job shop, *Management Science*, Vol. 30, No. 9, 1093-1104, [doi: 10.1287/mnsc.30.9.1093](https://doi.org/10.1287/mnsc.30.9.1093).
- [3] Udo, G.J. (1994). A simulation study of due-date assignment rules in a dynamic job shop, *Journal of the Operational Research Society*, Vol. 45, No. 12, 1425-1435, [doi: 10.1057/jors.1994.219](https://doi.org/10.1057/jors.1994.219).
- [4] Gordon, V.S., Proth, J.-M., Chu, C. (2002). Due date assignment and scheduling: SLK, TWK and other due date assignment models, *Production Planning & Control*, Vol. 13, No. 2, 117-132, [doi: 10.1080/09537280110069621](https://doi.org/10.1080/09537280110069621).
- [5] Modrák, V., Pandian, R.S. (2010). Flow shop scheduling algorithm to minimize completion time for n-jobs m-machines problem, *Tehnički Vjesnik – Technical Gazette*, Vol. 17, No. 3, 273-278.
- [6] Demir, H.I., Uygun, O., Cil, I., Ipek, M., Sari, M. (2015). Process planning and scheduling with SLK due-date

- assignment where earliness, tardiness and due-dates are punished, *Journal of Industrial and Intelligent Information*, Vol. 3, No. 3, 173-180, [doi: 10.12720/jiii.3.3.173-180](https://doi.org/10.12720/jiii.3.3.173-180).
- [7] Ojstersek, R., Brezocnik, M., Buchmeister, B. (2020). Multi-objective optimization of production scheduling with evolutionary computation: A review, *International Journal of Industrial Engineering Computations*, Vol. 11, No. 3, 359-376, [doi: 10.5267/j.ijiec.2020.1.003](https://doi.org/10.5267/j.ijiec.2020.1.003).
- [8] Janes, G., Perinic, M., Jurkovic, Z. (2017). An efficient genetic algorithm for job shop scheduling problems, *Tehnički Vjesnik – Technical Gazette*, Vol. 24, No. 4, 1243-1247, [doi: 10.17559/TV-20150527133957](https://doi.org/10.17559/TV-20150527133957).
- [9] Scrich, C.R., Armentano, V.A., Laguna, M. (2004). Tardiness minimization in a flexible job shop: A tabu search approach, *Journal of Intelligent Manufacturing*, Vol. 15, No. 1, 103-115, [doi: 10.1023/B:JIMS.0000010078.30713.e9](https://doi.org/10.1023/B:JIMS.0000010078.30713.e9).
- [10] Simchi-Levi, D., Wu, S.D., Shen, Z.-J.M. (2004). *Handbook of quantitative supply chain analysis: Modeling in the e-business era*, Springer Science & Business Media, New York, USA.
- [11] Wu, Z., Weng, M.X. (2005). Multiagent scheduling method with earliness and tardiness objectives in flexible job shops, *IEEE Transactions on Systems, Man, and Cybernetics, Part B (Cybernetics)*, Vol. 35, No. 2, 293-301, [doi: 10.1109/TSMCB.2004.842412](https://doi.org/10.1109/TSMCB.2004.842412).
- [12] Chen, B., Matis, T.I. (2013). A flexible dispatching rule for minimizing tardiness in job shop scheduling, *International Journal of Production Economics*, Vol. 141, No. 1, 360-365, [doi: 10.1016/j.ijpe.2012.08.019](https://doi.org/10.1016/j.ijpe.2012.08.019).
- [13] Ojstersek, R., Buchmeister, B. (2020). The impact of manufacturing flexibility and multi-criteria optimization on the sustainability of manufacturing systems, *Symmetry*, Vol. 12, No. 1, Paper No. 157, [doi: 10.3390/sym12010157](https://doi.org/10.3390/sym12010157).
- [14] Nie, L., Gao, L., Li, P., Li, X. (2013). A GEP-based reactive scheduling policies constructing approach for dynamic flexible job shop scheduling problem with job release dates, *Journal of Intelligent Manufacturing*, Vol. 24, No. 4, 763-774, [doi: 10.1007/s10845-012-0626-9](https://doi.org/10.1007/s10845-012-0626-9).
- [15] Rajabinasab, A., Mansour, S. (2011). Dynamic flexible job shop scheduling with alternative process plans: An agent-based approach, *The International Journal of Advanced Manufacturing Technology*, Vol. 54, No. 9-12, 1091-1107, [doi: 10.1007/s00170-010-2986-7](https://doi.org/10.1007/s00170-010-2986-7).
- [16] Gao, K.Z., Suganthan, P.N., Pan, Q.K., Chua, T.J., Cai, T.X., Chong, C.S. (2014). Pareto-based grouping discrete harmony search algorithm for multi-objective flexible job shop scheduling, *Information Sciences*, Vol. 289, 76-90, [doi: 10.1016/j.ins.2014.07.039](https://doi.org/10.1016/j.ins.2014.07.039).
- [17] Ma, D.Y., He, C.H., Wang, S.Q., Han, X.M., Shi, X.H. (2018). Solving fuzzy flexible job shop scheduling problem based on fuzzy satisfaction rate and differential evolution, *Advances in Production Engineering & Management*, Vol. 13, No. 1, 44-56, [doi: 10.14743/apem2018.1.272](https://doi.org/10.14743/apem2018.1.272).
- [18] Na, H., Park, J. (2014). Multi-level job scheduling in a flexible job shop environment, *International Journal of Production Research*, Vol. 52, No. 13, 3877-3887, [doi: 10.1080/00207543.2013.848487](https://doi.org/10.1080/00207543.2013.848487).
- [19] Xu, H., Bao, Z.R., Zhang, T. (2017). Solving dual flexible job-shop scheduling problem using a bat algorithm, *Advances in Production Engineering & Management*, Vol. 12, No. 1, 5-16, [doi: 10.14743/apem2017.1.235](https://doi.org/10.14743/apem2017.1.235).
- [20] Fu, H.C., Liu, P. (2019). A multi-objective optimization model based on non-dominated sorting genetic algorithm, *International Journal of Simulation Modelling*, Vol. 18, No. 3, 510-520, [doi: 10.2507/ijssimm18\(3\)co12](https://doi.org/10.2507/ijssimm18(3)co12).
- [21] Getachew, F., Berhan, E. (2015). Simulation and comparison analysis of due date assignment methods using scheduling rules in a job shop production system, *International Journal of Computer Science & Engineering Survey*, Vol. 6, No. 5, 29-40, [doi: 10.5121/ijcses.2015.6503](https://doi.org/10.5121/ijcses.2015.6503).
- [22] Ojstersek, R., Lalic, D., Buchmeister, B. (2019). A new method for mathematical and simulation modelling interactivity: A case study in flexible job shop scheduling, *Advances in Production Engineering & Management*, Vol. 14, No. 4, 435-448, [doi: 10.14743/apem2019.4.339](https://doi.org/10.14743/apem2019.4.339).
- [23] Yin, Y., Wang, D., Cheng, T.C.E. (2020). *Due date-related scheduling with two agents: Models and algorithms*, Springer Nature Singapore, Singapore, [doi: 10.1007/978-981-15-2105-8](https://doi.org/10.1007/978-981-15-2105-8).
- [24] Hajduk, M., Sukop, M., Semjon, J., Jánoš, R., Varga, J., Vagaš, M. (2018). Principles of formation of flexible manufacturing systems, *Tehnički Vjesnik – Technical Gazette*, Vol. 25, No. 3, 649-654, [doi: 10.17559/TV-20161012132937](https://doi.org/10.17559/TV-20161012132937).
- [25] Moslehi, G., Mahnam, M. (2011). A Pareto approach to multi-objective flexible job-shop scheduling problem using particle swarm optimization and local search, *International Journal of Production Economics*, Vol. 129, No. 1, 14-22, [doi: 10.1016/j.ijpe.2010.08.004](https://doi.org/10.1016/j.ijpe.2010.08.004).
- [26] Zhang, Y., Gong, D.-W., Ding, Z. (2012). A bare-bones multi-objective particle swarm optimization algorithm for environmental/economic dispatch, *Information Sciences*, Vol. 192, 213-227, [doi: 10.1016/j.ins.2011.06.004](https://doi.org/10.1016/j.ins.2011.06.004).